



O'zbekiston Respublikasi Ta'limni rivojlantirish
respublika ilmiy-metodik markazi

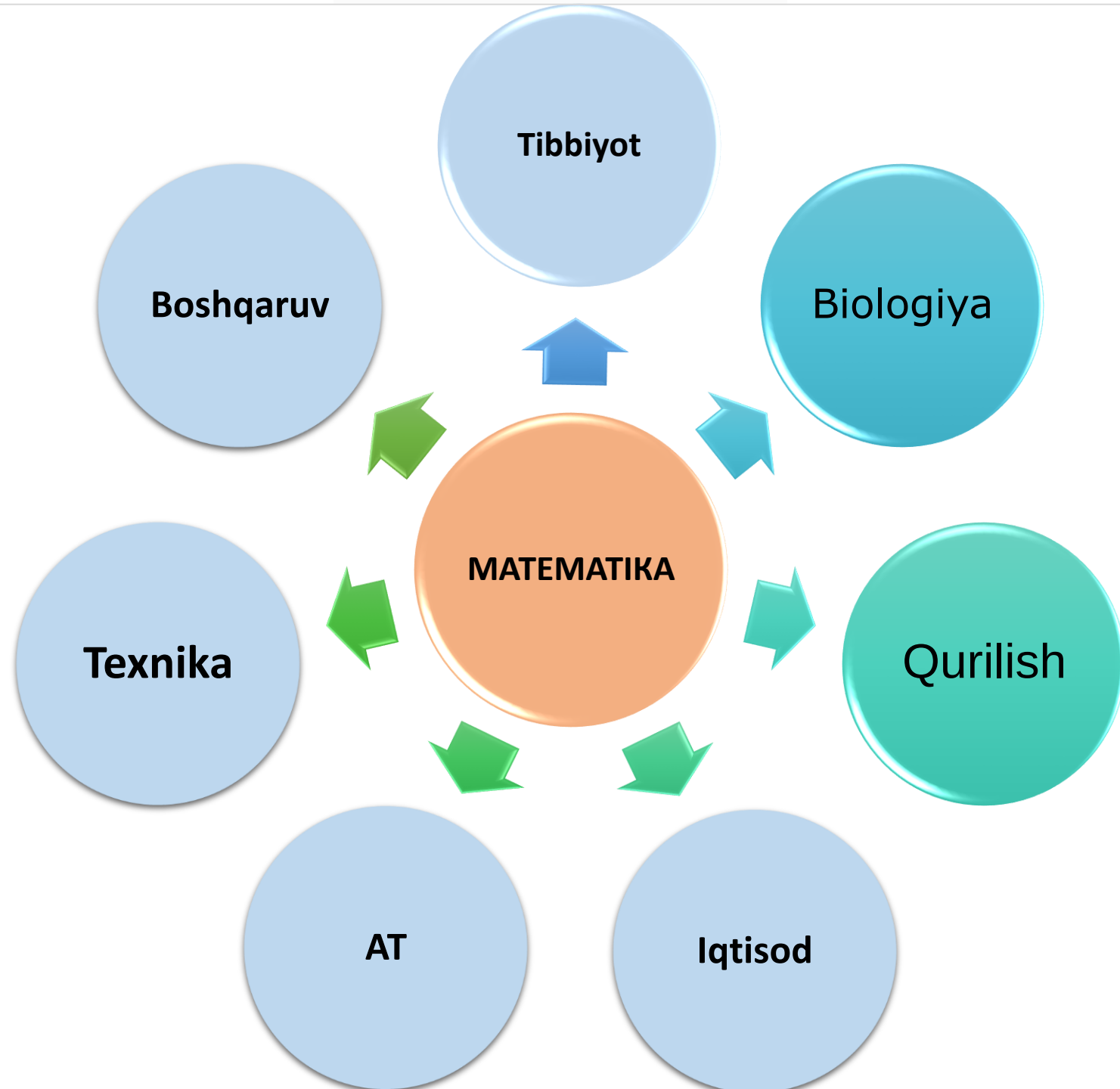
OLAMNI O'RGANISH VA UNI YAXSHILASHDA MATEMATIKADAN FOYDALANAMIZ"

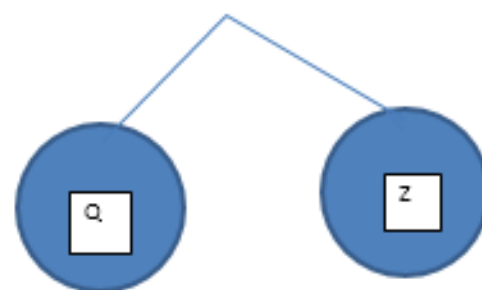
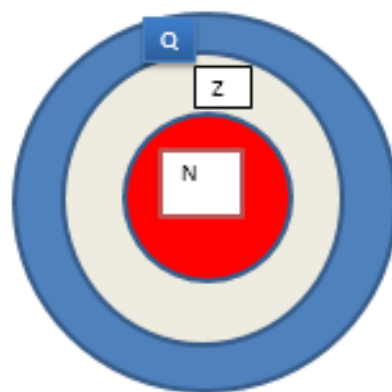
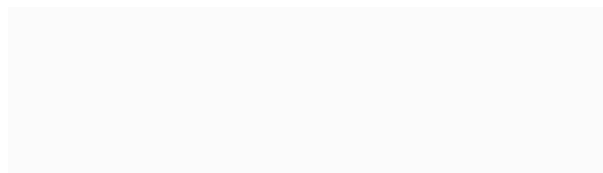
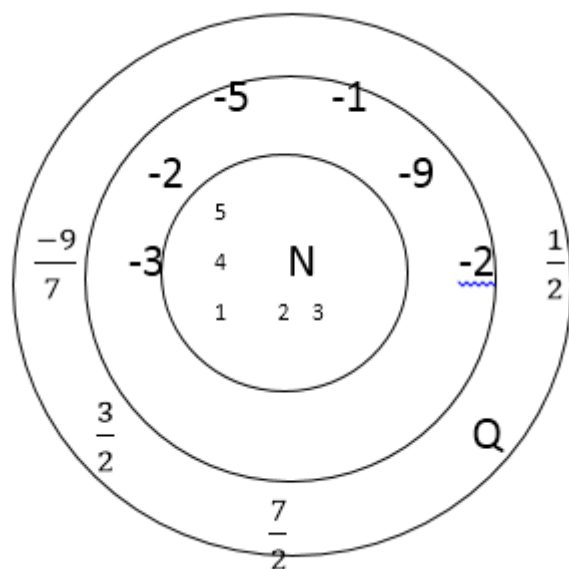
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TA'LIMDAGI O'ZGARISHLAR

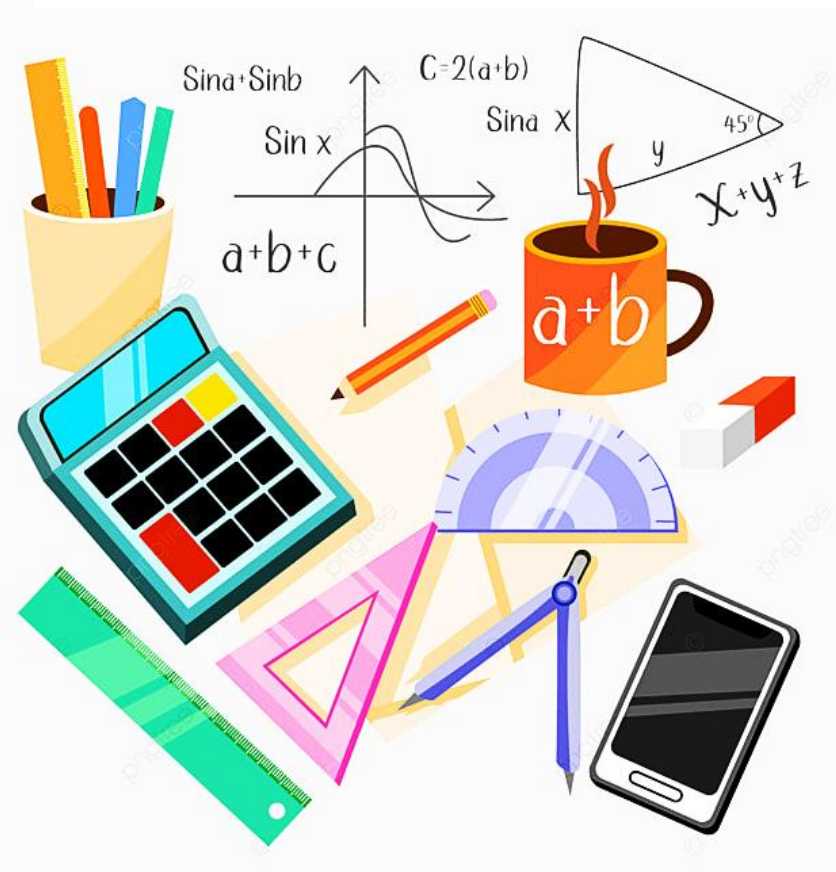
Mamlakatimizda ta'lim sohasiga katta e'tibor qaratilishi natijasida insonlarning yashash sharoitlari yaxshilanganligini ko'rish mumkin. Bizning mamlakatimizda ham ta'lim turli sohalarga yo'naltirilgan bo'lib rivojlangan mamlakatlar qatoriga kirishga harakat qilinmoqda. Ta'lim islohotlarining zamonaviy bosqichi jamiyatda yuz berayotgan yangilanishlarning tezkorligi, ta'lim muassalariga qo'yilayotgan yangi, yanada yuqori talablarga tezroq moslashish bilan bog'liq dolzarb vazifalarni ilgari surmoqda. O'zbekistonda ta'lim-tarbiya sohasini isloh qilishning asosiy omillaridan biri bu – ta'lim jarayoniga zamonaviy innovatsion va axborot-kommunikatsiya texnologiyalarini joriy etishdir



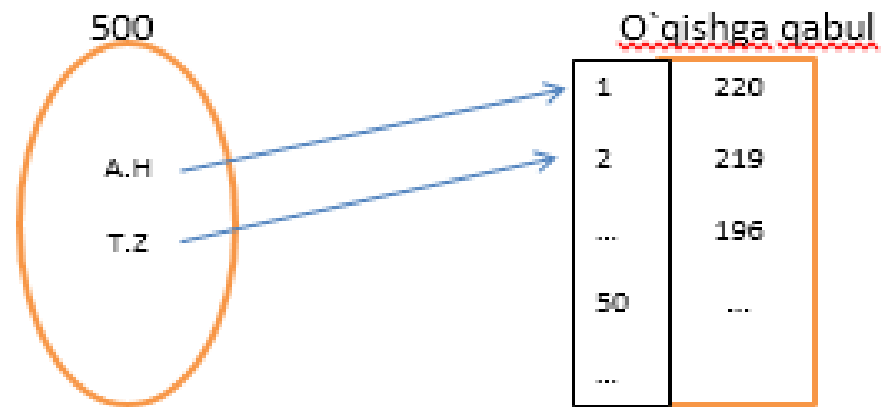




Ta'limga innovatsiyalar, yangi texnologiyalar kirib kelishi nafaqat ta'limni, balki, turli sohalarni rivojlanishiga imkon yaratadi. Davlatimiz aniq va tabiiy fanlarga, jumladan matematika faniga katta e'tibor qaratmoqda. Prezident maktablari, Al –Xorazmiy maktablarida matematika fani chuqur o'qitilmoqda. Matematika fanidagi mazmunni boyitishda tushunchalarning tatbiqlariga e'tibor qaratilsa, uning amaliy ahamiyati yanada yuqori bo'lar edi.

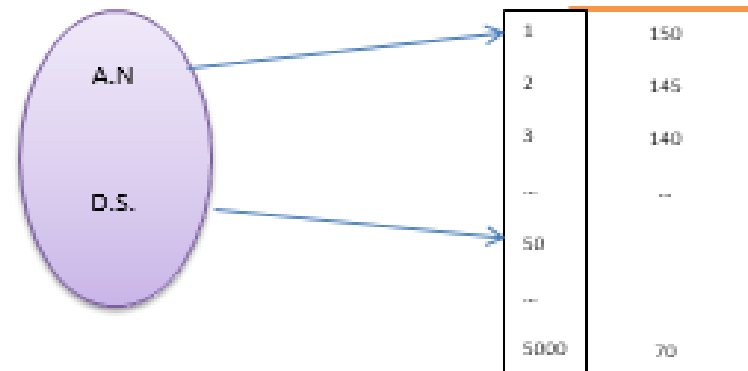


1-misol.



2-misol.

Xarbiy xizmatga yuborish. Xarbiy xizmatga bormog'chi bo'lgan o'g'il bolalar soni
500ta ulardan 50tasi xarbiy xizmatga borish kerak.



O'zbekiston Respublikasi Oliy ta'lim tizimini 2030- yilgacha rivojlantirish konsepsiyasida bir qator maqsadlar belgilab berilgan

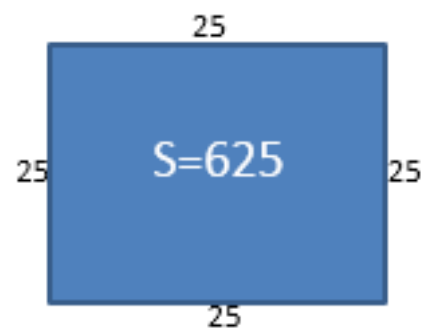
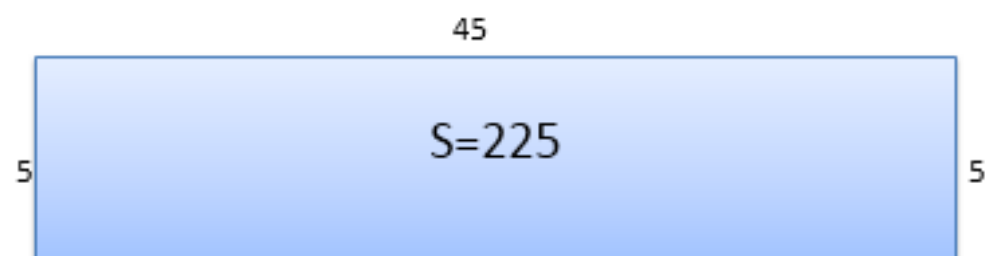
mamlakatni modernizatsiya qilish, ijtimoiy-iqtisodiy jihatdan barqaror rivojlantirish uchun yuqori malakali kadrlar tayyorlash sifatini oshirish, inson kapitalini mehnat bozori talablari asosida rivojlantirish;

oliy ta'lim bilan qamrov darajasini oshirish, xalqaro standartlar asosida yuqori malakali, kreativ va tizimli fikrlaydigan, mustaqil qaror qabul qila oladigan kadrlar tayyorlash, ularning intellektual qobiliyatlarini namoyon etishi va ma'naviy barkamol shaxs sifatida shakllanishi uchun zarur shart-sharoit yaratish;

sohada sog'lom raqobat muhitini shakllantirish, uning jozibadorligini oshirish, jahon miqyosidagi raqobatbardoshligini ta'minlash asosiy maqsadlardan qilib belgilandi.

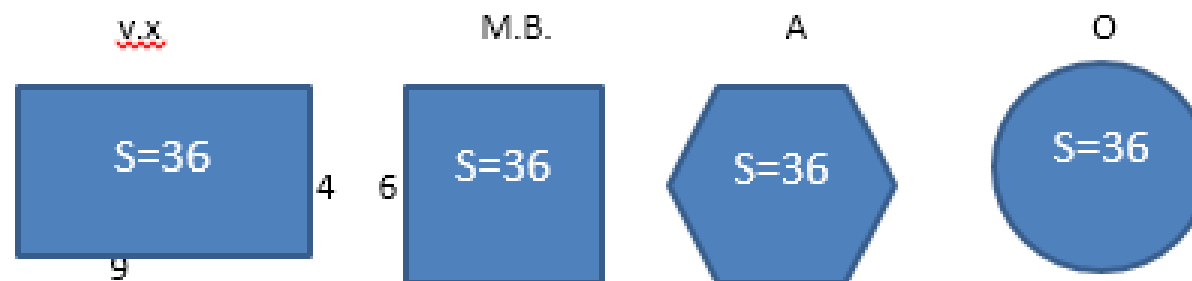
3-misol.

100 metrli argon bilan to'g'ri to'rtburchakli maydon o'rang.



4-misol.

Yuzasi 36 ga teng tekis maydonlar farqini taxlil qiling.



Bu shakllarni yuzasi bir xil bo'lgani bilan, lekin perimetri xar xil bo'lgani uchun ularni o'rash uchun ketadigan material har hil bo'ladi.

Masalan.

$$\text{V.X. } P = 2 \times (4 + 9) = 2 \times 13 = 26$$

$$\text{M.B. } P = 4 \times 6 = 24$$

$$\text{A. } P = 22$$

$$\text{O. } \pi R^2 = 36 \quad P = 2\pi R = 20$$







1. ATIRNING QUTISI QAYSI SHAKLDA TAYYORLANGANI MAQSADGA MUVOFIQROQ?



1-PARALELLIPEPID SHAKLIDAGI ATIR, AYTAYLIK ICHIGA 100ML
HAJMDAGI ATIR KETSIN, QUTISINI ISHLATISHGA $20CM^3$ SHISHA KETADI



PRIZMA SHALDAGI ATIRGA HAM, SHU HAJMDAGI SUYUQLIK KETADI,
AMMA QUTISIGA KAMROQ $18CM^3$ SHISHA ISHLATILADI

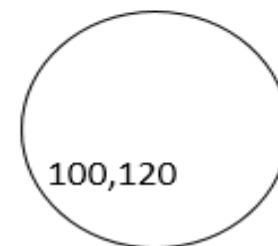
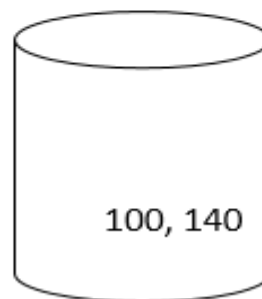
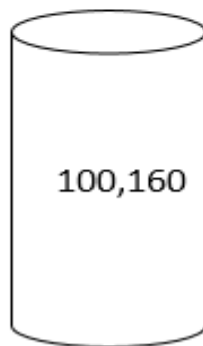
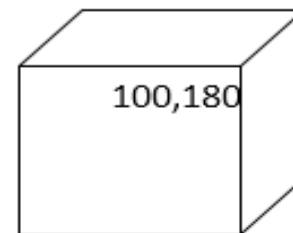
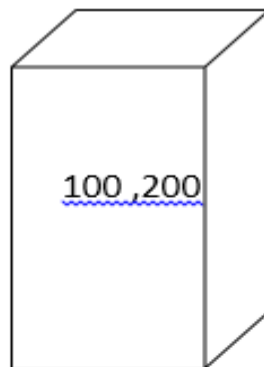


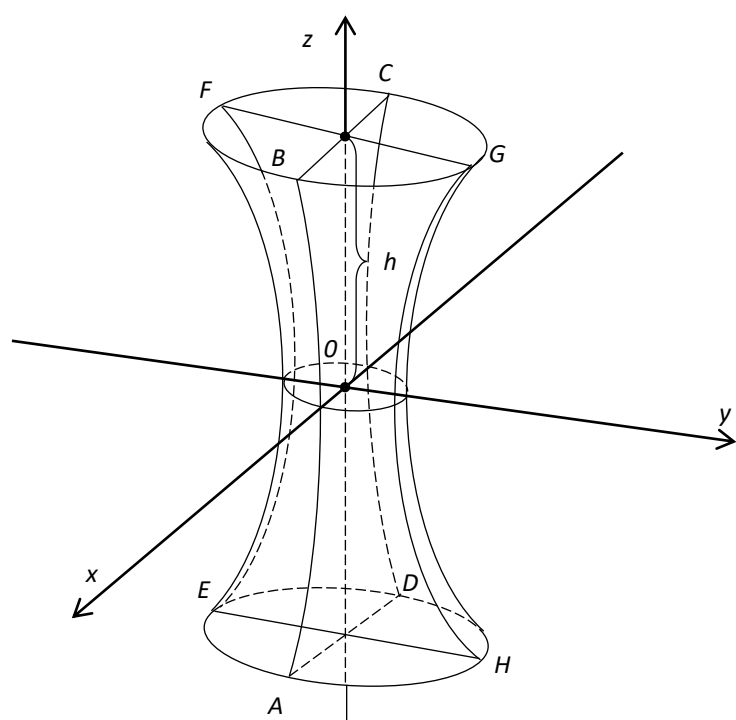
SLINDR SHAKLIDAGI PRIZMA SHAKLIDAGIDAN KAMROQ
 $16CM^3$ SHISHA KETADI



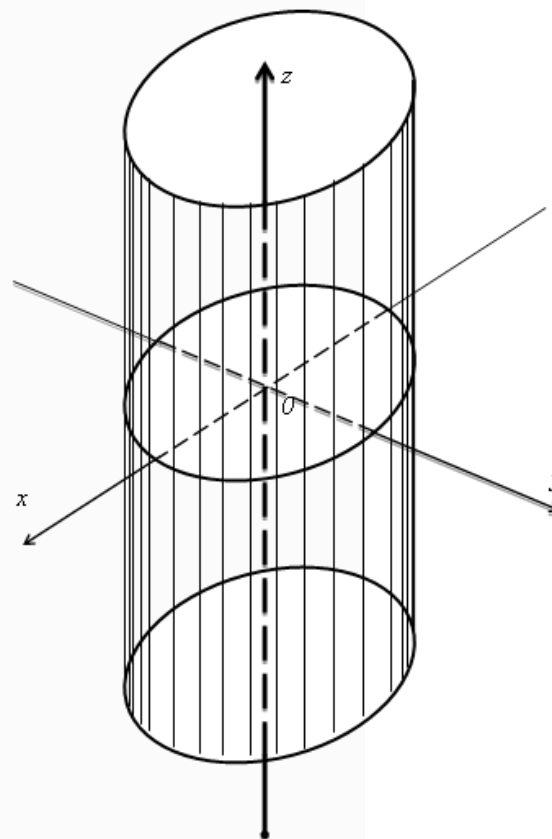
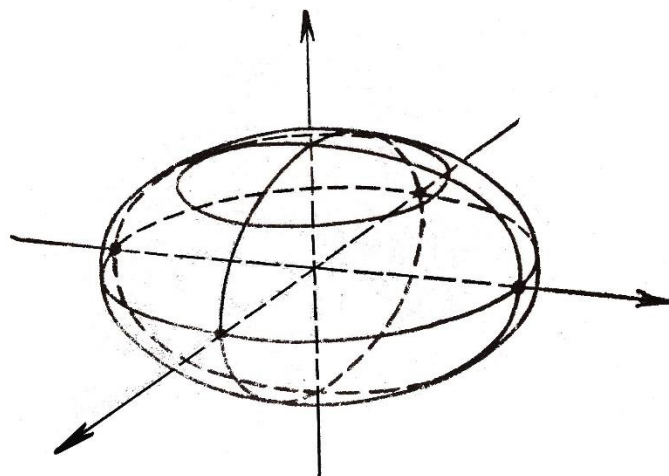
SHAR SHAKLIDAGI ATIRGA ESA, SUYUQLIK BIR XILKETADI, AMMO
 $14CM^3$ SHISHA KAMROQ KETADI

Geometrik fiquralar hajmi va to'la sirti

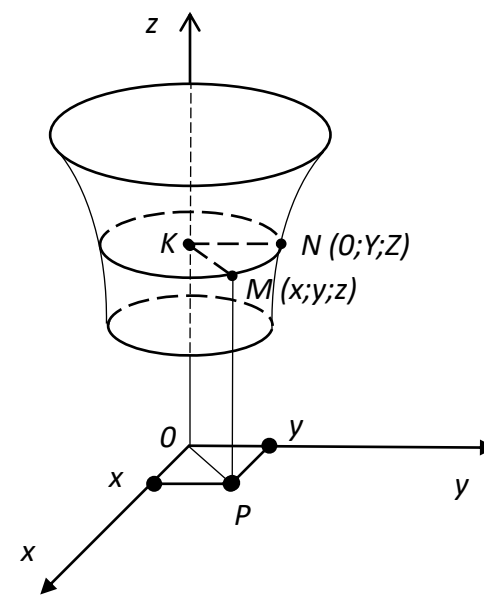




12-chizma



6-chizma



10-chizma

ROMAN NUMERALS

1. I	21. XXI	41. XLI
2. II	22. XXII	42. XLII
3. III	23. XXIII	43. XLIII
4. IV	24. XXIV	44. XLIV
5. V	25. XXV	45. XLV
6. VI	26. XXVI	46. XLVI
7. VII	27. XXVII	47. XLVII
8. VIII	28. XXVIII	48. XLVIII
9. IX	29. XXIX	49. XLIX
10. X	30. XXX	50. L
11. XI	31. XXXI	51. LI
12. XII	32. XXXII	52. LII
13. XIII	33. XXXIII	53. LIII
14. XIV	34. XXXIV	54. LIV
15. XV	35. XXXV	55. LV
16. XVI	36. XXXVI	56. LVI
17. XVII	37. XXXVII	57. LVII
18. XVIII	38. XXXVIII	58. LVIII
19. XIX	39. XXXIX	59. LIX
20. XX	40. XL	60. LX

ПОСТАВЬТЕ ЗНАК НИЖС ПОД НИЖИ

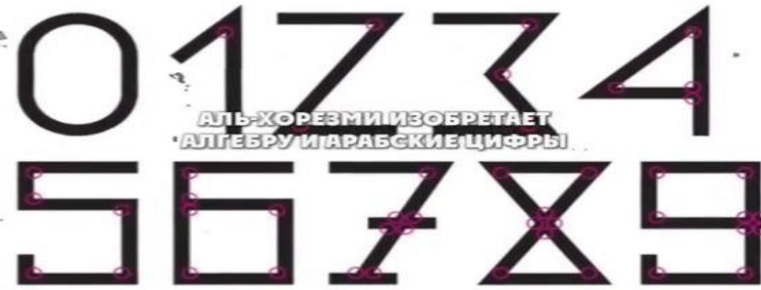
ROMAN NUMERALS: 1 TO 100

61. LXI	81. LXXXI
62. LXII	82. LXXXII
63. LXIII	83. LXXXIII
64. LXIV	84. LXXXIV
65. LXV	85. LXXXV
66. LXVI	86. LXXXVI
67. LXVII	87. LXXXVII
68. LXVIII	88. LXXXVIII
69. LXIX	89. LXXXIX
70. LXX	90. XC
71. LXXI	91. XCI
72. LXXII	92. XCII
73. LXXIII	93. XCIII
74. LXXIV	94. XCIV
75. LXXV	95. XCV
76. LXXVI	96. XCVI
77. LXXVII	97. XCVII
78. LXXVIII	98. XCVIII
79. LXXIX	99. XCIX
80. LXXX	100. C

И ПОПРОБУЙТЕ ВЫЧЕСТЬ РИМСКИЕ ЦИФРЫ ИЗ РИМСКИХ ЦИФР



SULTAN GIGLIO ©2017-2018



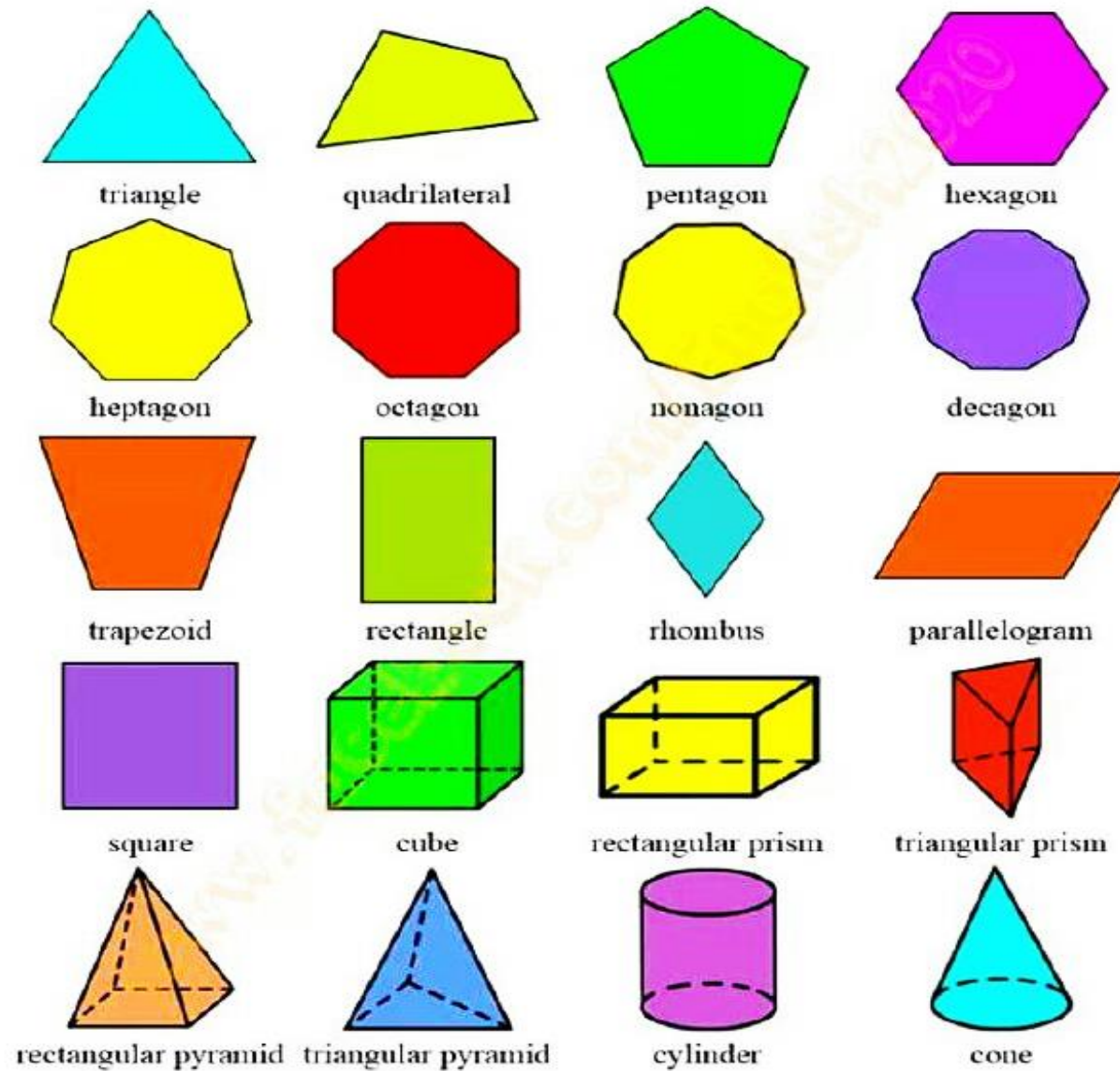
ARABIC NUMBERS NUMBERS & ANGLES

THE MATHEMATICIAN MUHAMMAD
IBN MUSA AL-KHWARIZMI (780-850)
DESIGNED ARABIC NUMBERS
BASED ON ANGLES.





Matematik savodxonlikni rivojlantiruvchi metodlar



6-misol.

Choynak ichlab chiqaradigan fabrikaning shishani tejab qolish uchun o'ylab topgan g'oyalari.

Bu fabrika ham birinchi bo'lib xuddi "Chanel" atir ishlab chiqaradigan fabrikaga o'xshab to'g'ri to'rtburchak shakli choynaklar ishlab chiqaradi.

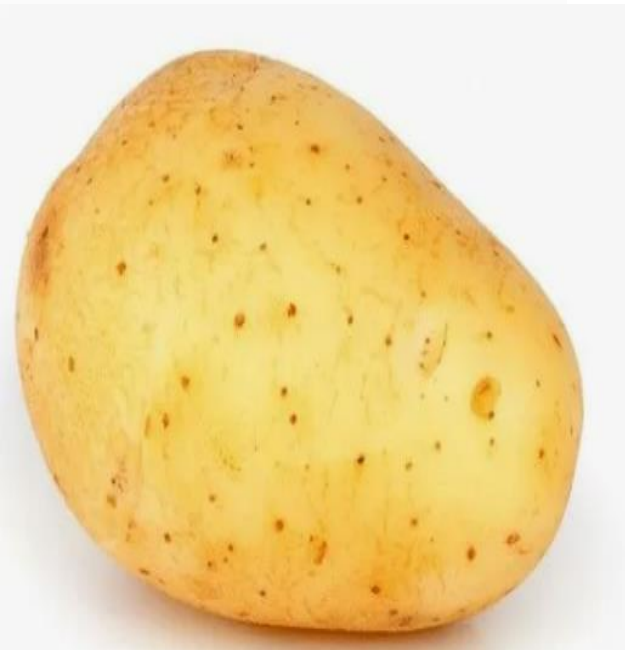


To'g'ri to'rtburchak choynaklaridan keyin choynak ishlab chiqarish fabrikasi silindr shaklidagi choynaklarni ishlab chiqa boshladi. Bu choynaklar to'g'ri to'rtburchak choynaklaridan ko'ra silindr shaklidagi choynaklarga kamroq shisha ketadi.



Silindr shakldagi choynaklarni ishlab chiqishga nisbatan shar shaklidagi choynakni ishlab chiqish chinnini tejashga olib keladi.







DUMALOQ KARTOSHKA PO`STLOG`INI ISTE`MOLGA YAROQLI BO`LISHI UCHUN ARCHGANIMIZDA, KAMROQ CHIQINDI CHIQADI. SHUNING UCHUN UNING SHAKLI DUMALOQ, BOSHQ SHAKLDA EMAS



OLCHA ISTE`MOLGA YAROQLI BO`LISHI UCHUN UNI YUVGANIMIZDA, SUV HAMMA TARAFIGA TEGISHI VA SUV KAM ISROF BO`LGANLIGI SABABLI, OLCHA DUMALOQ SHAKLDA

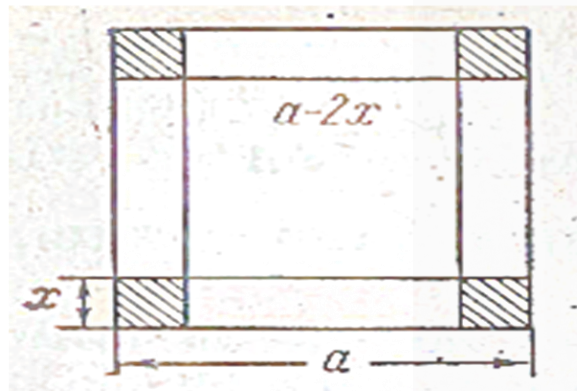
Vaziyatli topshiriqlar(keys qilish mumkin)

- Uzunligi 100 metrli to'g'ri to'rtburchak shaklidagi devor qurish lozim.
- Devor bilan o'ralgan maydon yuzasi qanday qiymatlarni qabul qila oladi?
- Eng katta yuzali maydonga ega bo'lish mumkinmi?
- Topshiriq. Maydon yuzasini maydon enining funksiyasi bo'lishini ko'rsating va uni tahlil eting.
- Eng katta yuzani aniqlang.

Vaziyatli topshiriqlar

- 18x18 o'lchamli, kvadrat shakldagi qattiq qog'oz berilgan. Uning burchaklaridan bir xil kvadratchalar qirqib olib, qolgan shakldan usti ochiq parallelepiped shakldagi quticha yasash talab qilinadi.
- Bu vaziyatni o'rganish uchun funksiyadan foydalaning.
- Har xil hajmli quticha yasash imkoni bormi?
- Eng katta hajmli quticha yasang.
- Topshiriq. Quticha hajmining qirqib olingan kvadratchalar tomonining funksiyasi bo'lishini ko'rsating va uni tahlil eting

3-misol. Tomoni a bo'lgan kvadrat tunukadan uning chekkalaridan bir hil kvadratchalar qirqib tashlab qolgan qismini buklab usti ochiq quticha yasash talab qilinadi. Hajmi eng katta bo'ladigan quticha yasash uchun qirqiladigan kvadratlarning tomoni qanday bo'lishi kerak? (5-chizma).



5-chizma

Yechilishi. Qirqib olinadigan kvadrat tomoni x ga teng bo'lsin, u holda yashikning tubini tashkil qiluvchi kvadratning tomoni $a - 2x$ ga teng. Yashikning hajmi:

$$V = (a - 2x)^2 x = a^2 x - 4ax^2 + 4x^3.$$

Masalani yechish uchun V funksiyaning $(0, a/2)$ intervaldagi eng katta qiymatini topish kerak. $V' = a^2 - 8ax + 12x^2$ hosilani topamiz. $a^2 - 8ax + 12x^2 = 0$ tenglamani yechib, ko'rsatilgan intervalga tegishli bo'lgan $x = a/6$ kritik nuqtani topamiz. $x = a/6$ nuqtada ikkinchi hosila $V'' = -8a + 24x$ manfiy bo'lgani uchun $[V''(\frac{a}{6}) = -8a + 24 \cdot \frac{a}{6} = -4a < 0]$, $x = a/6$ nuqtada V maksimumga erishadi:

$$V_{max} = \left(a - \frac{2a}{6}\right)^2 \frac{a}{6} = \frac{2}{27} a^3.$$

Tort uchun karobkadan guti yasash.

$$V=abc$$

$$a=18-2x$$

$$b=18-2x$$

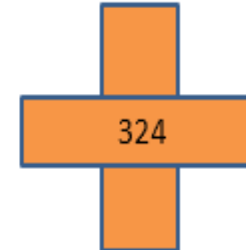
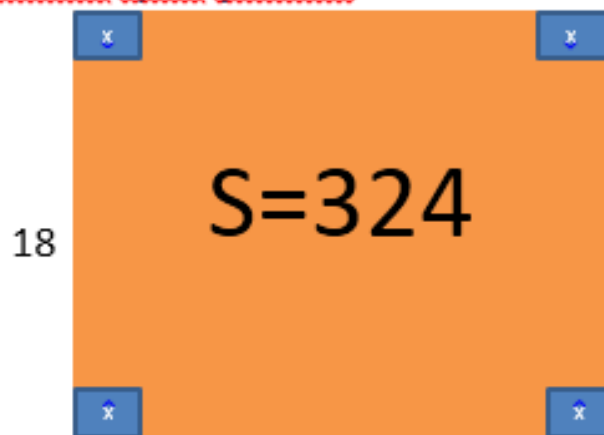
$$c=x$$

$$V=(18-2x)^2x$$

$$V(1)=256\text{cm}^3 \text{ dan gutidan } 4\text{cm}^2 \text{ chiqindi chqadi.}$$

$$V(2)=392 \text{ dan esa } 16 \text{ chiqindi}$$

$$V(3)=432 \text{ dan } 36 \text{ chiqindi.}$$



$$V>432$$

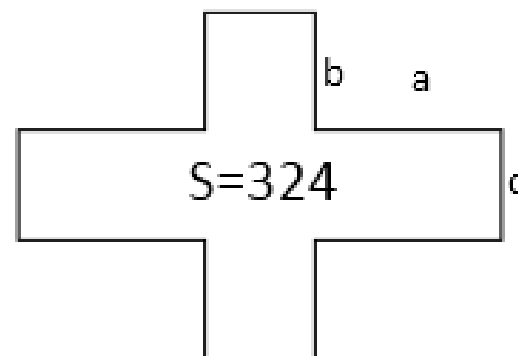
$$V>abc$$

$$ab+2bc+2ac=324$$

1-masala.

Bizga

Shu koʻrinishdagi figura berilgan. Bu figurani shunday joylashtirish kerakki. Hajmi eng katta boʻlgan idish yasash kerak.

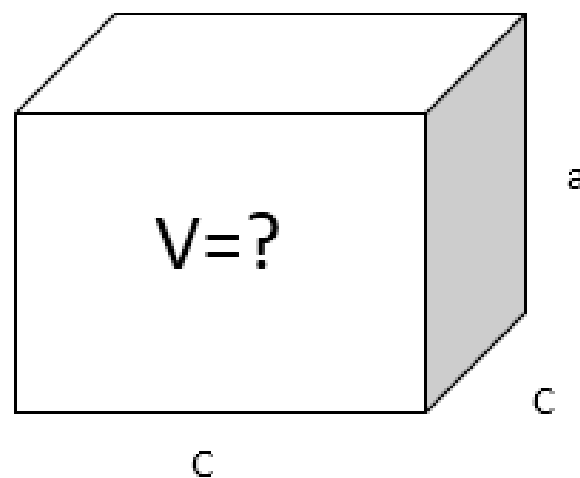


1-rasm

Bu figura hajmi eng katta boʻlishi uchun 1-rasmdagi figuradan $a=b$ shartni qanoatlantirish kerak.

Hajmi: $V = c^2 \cdot a$

$$S = c^2 + 4ac = 324 \quad a = \frac{324 - c^2}{4c}$$



$$S=c^2+4ac=324 \quad a=\frac{324-c^2}{4c}$$

Hosila olamiz, $V'=0$

$$\left(c^2 \cdot \frac{324-c^2}{4c}\right)'=0$$

$$\left(\frac{324c-c^3}{4}\right)'=0$$

$$324 = 3c^2 \quad a = \frac{216}{24\sqrt{3}} = 3\sqrt{3}$$

$$c^2 = 108$$

$$c = 6\sqrt{3}$$

$$V = 108 \cdot 3\sqrt{3} = 324\sqrt{3} \approx 561.184$$

Xulosa: Agar a tomon $3\sqrt{3}$ va c tomon $6\sqrt{3}$ ga teng bo'lganda hajmi eng katta bo'lgan idish yasash mumkin.

Javob: $V = 561.184$

2-misol.

Bizga berilgan figuraning eng katta hajmga ega bolishini ko`rib o`tsak.

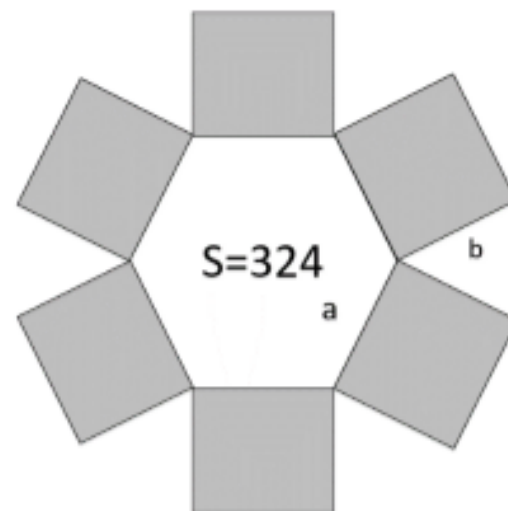
Bu figuraning yuzasi:

$$S = 6ab + \frac{3\sqrt{3}a^2}{2} = 324$$

Bu tenglikdan b ni a orqali ifodalab olamiz.

$$b = \frac{216 - \sqrt{3}a^2}{4a}$$

Ko`rinishida ifodalab oldik.



Endi biz berilgan figuraning eng katta hajmini hisoblab olamiz.

Hajmi formulasi:

$$V = \frac{3\sqrt{3}}{2} a^2 \cdot b$$

Formula yordamida topiladi.

Eng katta hajmga ega bo'lishi uchun

$$V' = 0$$

Shart bajarilishi kerak.

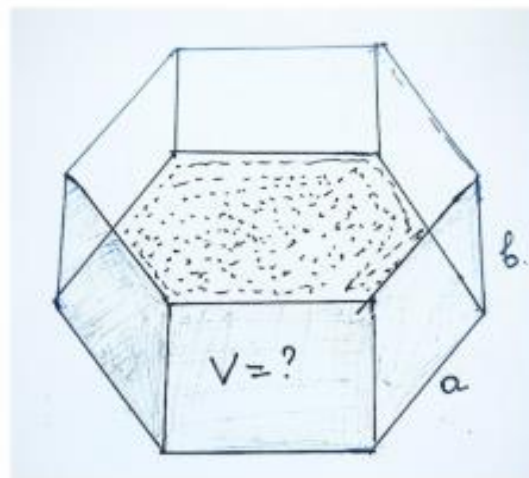
$$\left(\frac{3\sqrt{3}}{2} \cdot a^2 \cdot \frac{216 - \sqrt{3}a^2}{4a} \right)' = 0 \quad 324\sqrt{3} - 13,5a^2 = 0$$

$$a = 2\sqrt{6\sqrt{3}} \quad b = 3\sqrt{2\sqrt{3}}$$

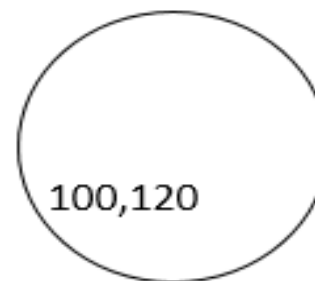
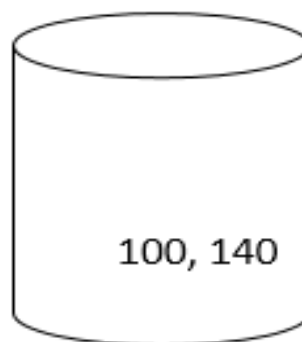
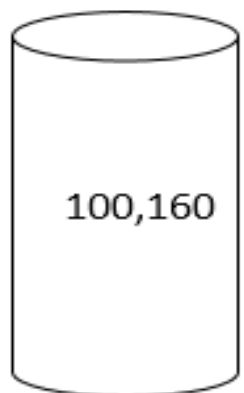
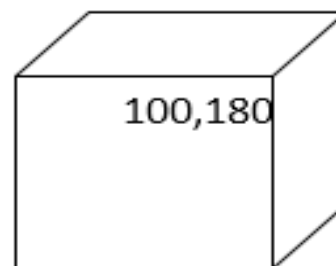
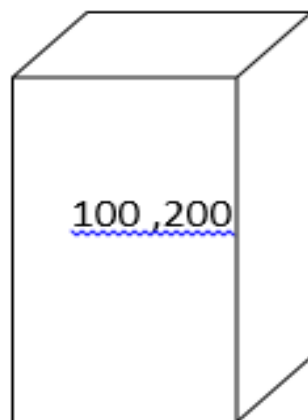
Hajmi:

$$V = \frac{3\sqrt{3}}{2} a^2 \cdot b = \frac{3\sqrt{3}}{2} \cdot 24\sqrt{3} \cdot 3\sqrt{2\sqrt{3}} = 324\sqrt{2\sqrt{3}} = 603.031$$

Javob: $V = 603.031$



Geometrik fiquralar hajmi va to'la sirti



To'la sirti 324 cm^2 bo'lgan yarim sfera olaylik



$$\frac{S}{2} = 4\pi R^2 \cdot \frac{1}{2} = 324 \text{ cm}^2 \quad 2\pi R^2 = 324 \text{ cm}^2 \quad \pi R^2 = 162 \text{ cm}^2$$

$$R^2 = \frac{162}{\pi} \approx 51 \quad \underline{R \approx 7} \quad \frac{V}{2} = \frac{4}{3}\pi R^3 \cdot \frac{1}{2}$$

Formulaga ko'ra

$$\frac{V}{2} = \frac{4}{3}\pi \cdot 7^3 \cdot \frac{1}{2} \approx 700 \text{ cm}^3$$

sferaning $\frac{1}{8}$ qismi olinsa

$$\frac{S}{8} = 4\pi R^2 \cdot \frac{1}{8} = 324 \text{ cm}^2 \quad \frac{1}{2}\pi R^2 = 324 \text{ cm}^2$$

$$\pi R^2 = 648 \text{ cm}^2$$

$$R^2 = \frac{648}{\pi} \approx 206$$

$R \approx 14$ bo'ladi. Formulaga ko'ra

$$\frac{V}{8} = \frac{4}{3}\pi R^3 \cdot \frac{1}{8}$$

$$\frac{V}{8} = \frac{4}{3} \cdot \pi \cdot 14^3 \cdot \frac{1}{8} \approx 1436 \text{ cm}^3$$

Hajmga ega bo'lamiz

$$\frac{S}{16} = 4\pi R^2 \cdot \frac{1}{16} = 324 \text{ cm}^2$$

$$\frac{1}{4}\pi R^2 = 324 \text{ cm}^2$$

$$\pi R^2 = 1296 \text{ cm}^2$$

$$R^2 = \frac{1296}{\pi} \approx 412$$

$$R \approx 20$$

$$\frac{V}{16} = \frac{4}{3}\pi R^3 \cdot \frac{1}{16}$$

$$\frac{V}{16} = \frac{4}{3} \cdot \pi \cdot 20^3 \cdot \frac{1}{16} \approx 2094 \text{ cm}^3$$

E'TIBORINGIZ UCHUN RAXMAT!